

DO THE MATH TEACHER GUIDE **SAMPLER**

FRACTIONS

This Sampler includes select pages from the Fractions Teacher Guide. You'll see a sample of the:

- Section Overview
- Instructional Principals
- Letter from Marilyn Burns
- Planner
- Lessons
- Annotated WorkSpace
- Attitude Survey, Show What You Know, Objectives Tracker, Community News





To see additional *Do The Math* samplers, please visit http://hein.pub/DoTheMathSamplers

To access the eSampler, please visit Heinemann.com/DoTheMath.



Overview

Introduction to Do The Math

An Introduction From Marilyn Burnsiv	I
Instructional Principlesv	i
Fractions 🕒 Materials	(
Fractions 🕒 at a Glancexiv	/
Table of Contents xv	i

> The Lessons

PAGE

LESSONS 1-5

Introduce Comparing

Fractions Students use fraction kits as they begin to develop a Comparing Fractions Toolkit. The first two strategies are compare unit fractions and compare fractions with common numerators.



LESSONS 6-10

Name Fractional Parts of Sets

fractions to include fractions of a set.

PAGE Students learn another strategy from the 5 Comparing Fractions Toolkit—compare fractions with common denominators. They also expand their understanding of

LESSONS 11-15

Identify Fractions Equivalent to $\frac{1}{2}$ PAGE

Students learn a strategy from the Comparing Fractions Toolkit—compare fractions to *1 whole*. They also use the relationships between numerators and denominators to identify fractions equivalent to $\frac{1}{2}$.



LESSONS 16-20

Compare Fractions to $\frac{1}{2}$

PAGE

Students learn another strategy from the Comparing Fractions Toolkit—compare fractions to $\frac{1}{2}$. They use cube trains to identify whether fractions of a set are less than, equal to, about equal to, or greater than $\frac{1}{2}$.



PAGE

Rename Fractions With Equivalent Fractions Students learn the last strategy from the

Comparing Fractions Toolkit—change fractions to equivalent fractions. They use both their fraction kits and circles to identify equivalent fractions.



PAGE

Compare and Order Fractions

Students use all of the strategies in the Comparing Fractions Toolkit to compare and order fractions, including improper fractions. Through the creation of a fraction concept web, students review fraction concepts and vocabulary, and make connections.



> Additional Resources

Attitude Survey	
Objectives Tracker	
Do The Math Community News	
Teacher Glossary	
Index	





141			•	•	
142			•	•	
143					
149					
154				•	





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J			
J			
J			
J			
J			
J			
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Instructional Principles

Help At-Risk and Struggling Students **Succeed in Math**

Research shows that students with diverse needs succeed in learning mathematics through explicit, intentional teaching based on proven instructional strategies.

TEACHING FOR UNDERSTANDING

Students benefit from instruction based on teaching for understanding.

Step-by-step lessons help students develop understanding, learn mathematical skills, see relationships, and make connections.

- Learning experiences link concepts and skills to their mathematical representations and language.
- Students use concrete and pictorial models to build a strong foundation in key mathematical concepts, operations, and strategies.

<u>1</u> 2

SCAFFOLDED CONTENT

Scaffolding of the content makes the mathematics more accessible to students.

Do The Math focuses on key content in mathematics so that students are not overwhelmed with extraneous material.

- The content is organized into manageable chunks.
- The lessons are explicit about the relationships among these chunks.
- The instruction is carefully sequenced to help students build a solid foundation of understanding.

FRACTIONS MODELS



Fraction strips help Fraction cards students to identify are used to order fractions and fractions from least understand fraction to greatest. equivalence



Connecting cubes create fraction trains and represent parts of a set.



Fraction circles are Fraction cubes divided to represent determine sharing problems. random numbers in fraction games.

MULTIPLE STRATEGIES

Exploring different strategies for developing concepts and skills builds students' reasoning.

The lessons engage students with each concept and skill in several ways, deepening their mathematics knowledge.

- Hands-on manipulatives give students concrete experiences with abstract ideas.
- The digital mTools give students the opportunity to translate concrete manipulatives to pictorial representations.
- Classroom and digital partner games offer engaging experiences that reinforce mathematical understandings and skills.
- Children's literature provides a springboard for instruction.
- Contexts make abstract mathematical ideas accessible.





Teacher Guide ted by Marilyn Burn



MATHEMATICAL THINKING

These standards help develop mathematical expertise and habits of mind in all students.

Students persevere and solve problems and look for entry points to solutions.

Students reason abstractly to make sense of quantities and their relationships in problem situations.

 Students use stated assumptions, definitions, and previously established results to construct viable arguments.

Students model with mathematics to solve real-world and mathematical problems.

Students apply mathematical and practical tools strategically when solving problems.

Students attend to precision, using mathematical language to communicate clearly and accurately.

Students look closely to **discern patterns** or structure when solving problems.

Students use repeated reasoning to identify general methods and shortcuts.



Instructional Principles (continued)

Help Students Build Their **Mathematical Reasoning**

CLASSROOM ROUTINES

INDEPENDENT STUDENT WORK

Routines such as "think, pair, share" promote engagement and deepen student understanding.

THINK Students collect their thoughts individually.

PAIR Students discuss with a partner.

SHARE Students report ideas to the whole group. Expressing ideas and hearing other perspectives

help students clarify their thinking.

- The listening and speaking that occur during "think, pair, share" are especially valuable for English language learners.
- Teachers can pair English language learners with other students who speak the same first language to allow them to discuss concepts.
- Teachers can also pair a student with early English skills and a student with strong English skills to encourage language development.

Assignments provide students with opportunities to practice, strengthen, and extend their learning.

- WorkSpace® assignments are carefully constructed to motivate students and maximize their success through games, assignments for reinforcement, and problem-solving situations.
- The digital experience gives students the flexibility to explore mathematical tools and games within and outside the classroom.

VOCABULARY AND LANGUAGE

Explicit vocabulary instruction helps students communicate effectively about the math they are learning.

Vocabulary is introduced after students experience concepts. Vocabulary lessons follow a consistent routine-the teacher writes the vocabulary on the Math Vocabulary chart and provides an example; students see, hear, say, and write it; the vocabulary is then incorporated throughout the lessons to support students' learning.

- Key mathematical and academic vocabulary is highlighted at the start of each lesson, and Spanish translations are provided.
- A **glossary** in the *WorkSpace*[®] provides students with a reference for definitions.



Explain c





ASSESSMENT AND DIFFERENTIATION

Ongoing assessment is built into the program to help teachers meet individual student needs.

During lessons, teachers observe students working in the whole group, with partners, and independently.

Specific guidance for how to promote understanding and address student misconceptions is integrated into all lessons.

Suggestions for differentiating instruction are included after every "Assessing Student Understanding" lesson, both for students who need additional help and those who are ready for a challenge.



Teacher Guide eated by Marilyn Burns





FROM MARILYN BURNS

Dear Colleague,

Students now learn the third strategy in the Comparing Fractions Toolkit comparing fractions with common denominators. For this strategy, students compare two fractions with the same denominator. First they review that fractions with the same denominator each represent 1 whole cut into the same number of equal pieces. Then they reason that the fraction with the greater numerator has more pieces and, therefore, is the greater fraction. Finally they confirm by comparing with their fraction kit pieces.

6 5

In	Lessons 6	5–10,
stu	dents	

- Compare fractions with common numerators and with common denominators.
- Name parts of a set as fractions and use standard notation.
- · Solve problems using fractions.
- · Communicate ideas with key math vocabulary: numerator. common numerator, denominator, unit fraction, and common denominator.

$\frac{6}{8} > \frac{6}{8}$								
			1					
10	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{8}$			
$\frac{1}{8}$	$\frac{1}{8}$	1/8	$\frac{1}{8}$	$\frac{1}{8}$				

The lessons also engage students in relating fractions to parts of sets, rather than parts of a single whole. The illustrations in the book How Many Snails? provide contexts for identifying the numerators and denominators of fractional parts of sets. Each spread in the book presents questions that ask readers to observe differences among sets of similar objects-clouds, flowers, fish, trucks, books, and others. The questions in the book were written with the intention of being answered with whole numbers; however, for these lessons, they are reworded so that students respond with answers that are fractions.

 $\frac{3}{8}$ of the 8 clouds are big and fluffy.

 $\frac{4}{8}$ of the 8 clouds are white.



Name Fractional Parts of Sets

26

Learn more at **Heinemann.com/DoTheMath**











LESSON

(10

Progress Monitoring

Assessing Student Understanding

Students demonstrate understanding of the objectives of Lessons 6–9 by completing WorkSpace pages independently.

- Compare fractions with common numerators and common denominators.
- Name parts of sets as fractions and use standard notation.
- Represent fractional parts of sets with drawings and fractions.
- Solve problems using fractions.

Assessing with visual models and symbol ion they have been using in Lessons

6-9 allows students to show their understanding without having to approach the material in an unfamiliar format.

- common denominator
- is greater than

- is less than common numerator
 • unit fraction

Planner 29

- WorkSpace pages 16-17 and 49
- Fraction strips
- Red and blue fraction cubes
- Uncover 😭

















Next Lesson Students learn a new strategy for comparing fractions-comparing fractions that

SPAC	E PAG	ìΕ	16
What Yor we strategies to com gy 1: compare unit gy 2: compare frac gy 3: compare frac gy 3: compare frac or > between each	u Know pare each pair of fract fractions $\left[\frac{1}{2} > \frac{1}{2}\right]$ tions with common de to pair.	tions. merato	tors $\left[\frac{1}{2}, \frac{1}{2}\right]$ nations $\left[\frac{1}{2}, \frac{1}{2}\right]$
<u>2</u> 10	٥	1 5 <	< 1/4
<u>3</u> 9	۲	<u>5</u> >	• <u>5</u>
18	6	3 >	▶ 2 8
1	8	48 <	< \$
11 12	9	8 10	> 8/12





The Attitude Survey measures students' disposition towards math.

LESSON (10) Assessing Student Understanding

ASSESSMENT Progress Monitoring

Objectives

- · Compare fractions with common numerators and common denominators.
- Name parts of sets as fractions and use standard notation.
- Represent fractional parts of sets with drawings and fractions.
- Solve problems using fractions.
- Communicate ideas with key math vocabulary: common numerator, unit fraction, and common denominator.

Assess

Use the annotated pages to correct *WorkSpace* pages 16 and 17.



Note the progress of each student in the appropriate rows on the tracking chart on page 142.

Differentiating Instruction

Although the lessons are carefully scaffolded and paced at a rate most likely to give students a chance for optimal learning, there will be instances when some students are still struggling and need extra support. Likewise, there will be instances when some students would benefit from additional challenges or practice. Try the teaching ideas below.

For Students Who Need More Support

• If students have difficulty comparing fractions using the three toolkit strategies that have been presented, have them practice comparing fractions that can be verified with their fraction strips. Have students think and predict which fraction will be greater, then check using the fraction strips.

For Students Ready for a Challenge

• Have students grab a handful of change and use it to describe parts of a set.



In this example, the set of coins can be described in the following ways:

- $=\frac{4}{10}$ quarters
- $=\frac{6}{10}$ pennies
- $=\frac{7}{10}$ heads
- $=\frac{3}{10}$ tails

Students can ask each other questions about their sets of coins. It is easy to grab different handfuls of coins to come up with many different sets and fractions of sets.

ATTITUDE SURVEY

Name:

1

2

3

4

5

> Fill in the circle of the answer that best fits you.

I like meth	6 Thalia
• I like math.	be solv
	⊖ ag
	⊖ ag
Some, but it's not my favorite	ige ⊖
○ it's my favorite subject	
I am good at math	U uis
\bigcirc not at all	> Which
\bigcirc not very good	You ma
\bigcirc fairly good	7. When n
	⊖ tak
	() giv
. I need good math skills so I can get	
a good job when I am older.	
⊖ agree a lot	⊖ asl
⊖ agree a little	U dist
\bigcirc disagree a little	► Write a
⊖ disagree a lot	<mark>8.</mark> What d
. I can get better in math if I work hard.	
🔿 agree a lot	
\bigcirc agree a little	
🔿 disagree a little	
🔿 disagree a lot	
. I like solving different problems.	9. What d
⊖ agree a lot	
🔿 agree a little	
🔿 disagree a little	
🔿 disagree a lot	

46 Name Fractional Parts of Sets

Date:

eve that math problems can often ved using different strategies.

- ree a lot
- ree a little
- sagree a little
- sagree a lot

of these do you agree with? ay choose more than one answer.

nath is challenging, I $_$

- ke on the challenge.
- ve up easily.
- ut in a little effort.
- ut in a lot of effort.
- sk my teacher for help.

an answer to each question.

do you like most about math? Explain.

do you like least about math? Explain.

141







Students complete "Show What You Know" assignments every fifth lesson. These assignments help you monitor student progress and assess understanding of the concepts and skills from the previous four lessons.

Show What You Know

DIRECTIONS

> Use these strategies to compare each pair of fractions. **Strategy 1:** compare unit fractions $\frac{1}{6} > \frac{1}{8}$ **Strategy 2:** compare fractions with common numerators $\frac{3}{12} < \frac{3}{4}$ **Strategy 3:** compare fractions with common denominators $\frac{1}{4} < \frac{2}{4}$ ➤ Write < or > between each pair. (1) $\frac{2}{7} > \frac{2}{10}$ (2) $\frac{1}{5} < \frac{1}{4}$

(3) $\frac{2}{9} < \frac{3}{9}$	$(4) \ \frac{5}{4} > \frac{5}{6}$
(5) $\frac{1}{3} > \frac{1}{8}$	$(6) \ \frac{3}{8} > \frac{2}{8}$
$7 \frac{1}{16} < \frac{1}{11}$	(8) $\frac{4}{8} < \frac{4}{5}$
$9 \frac{7}{12} < \frac{11}{12}$	(10) $\frac{8}{10} > \frac{8}{12}$
16 Lesson 10 Home Note: Your child compared using three strategies he or she	res fractions e has learned.

> Draw the whole set and mark the fractional p	art.
1 $\frac{2}{3}$ of a set of circles are shaded.	2
$3\frac{4}{5}$ of the squares are red.	4
(5) $\frac{5}{6}$ of the triangles have an X.	6

Home Note: Your child makes drawings to represent fractional parts of sets.





Connecting Home to School: Send hor
The Math Community News letters bef
of five lessons to encourage family i

Objectives Tracker

FRACTIONS B

142

> Record the date in the appropriate box as students are assessed on each of the objectives. When the student consistently performs an objective with accuracy, add a checkmark to the box.

MODULE OBJECTIVES	JIUDENT NAMES	/ /	, /	, /	, /	, /	, /	
Name parts of a whole and parts of a set as fractions and use standard notation.								
Compare and order fractions using benchmarks, common numerators, common denominators, and fractions one unit fraction away from 1 whole.								
Identify equivalent fractions.								
Solve problems using fractions.								
Communicate ideas with key math vocabulary: numerator, common numerator, denominator, unit fraction, improper fraction, mixed number, equivalent, and common denominator.								

Community News Do lhe Math Notes of interest to the classroom teachers and families of students participating in the Do The Math program FRACTIONS (B) Equivalence and Comparison LESSONS 1-5 **UPDATE:** Students learn strategies for comparing fractions with the same numerator. For example, they learn that $\frac{1}{4}$ is greater than $\frac{1}{8}$ and $\frac{2}{3}$ is greater than $\frac{2}{5}$.

Fraction Flags

Ŧ

> Here is an activity that will give your child practice comparing fractions.

In each of the flags below, part of the flag is white. Write a fraction for the white part of each flag. Then put the fractions in order from least to greatest.

Here is a hint: write each fraction with the same numerator, 2.

me copies of Do fore each group involvement.



143



